

Solubilities of actinides in complex solutions

What are the solubility controlling phases in complex media?

Pierre Vitorge, Catherine Beaucaire, Marie-Hélène Fauré, Serge Maillard:
CEA-Saclay.contact.pierre.vitorge(at)cea.fr.
Hélène Capdevila: CEA Cadarache.

1 - "Simple" case Na / Np(V) / carbonate system

Solubility *Ch.Dautel, P.Vitorge, I.Grenthe, D.Ferri*

Solid solution (NpO_2^+ / Na^+ ionic exchange)?

P.Vitorge, M.-H.Fauré, S.Maillard

Sorption on a clayey sand (NpO_2^+ / H^+ ionic exchange)

Ch.André (thesis), P.Vitorge, M.Sardin (LSGC CNRS ENSIC Nancy)

2 - Ligand competition in solid compounds

Am solubility in $\text{OH}^-/\text{CO}_3^{2-}/\text{HCO}_3^-/\text{CO}_2$ aqueous solutions

P.Vitorge, E.Giffaut (thesis), P.Robouch

3 - Redox reactions

Np(IV) solubility in $\text{OH}^-/\text{CO}_3^{2-}/\text{HCO}_3^-$ aqueous solutions

P.Vitorge (TDB NEA-OECD)

PuO_2 (hyd,am) solubility product

H.Capdevila, P.Vitorge

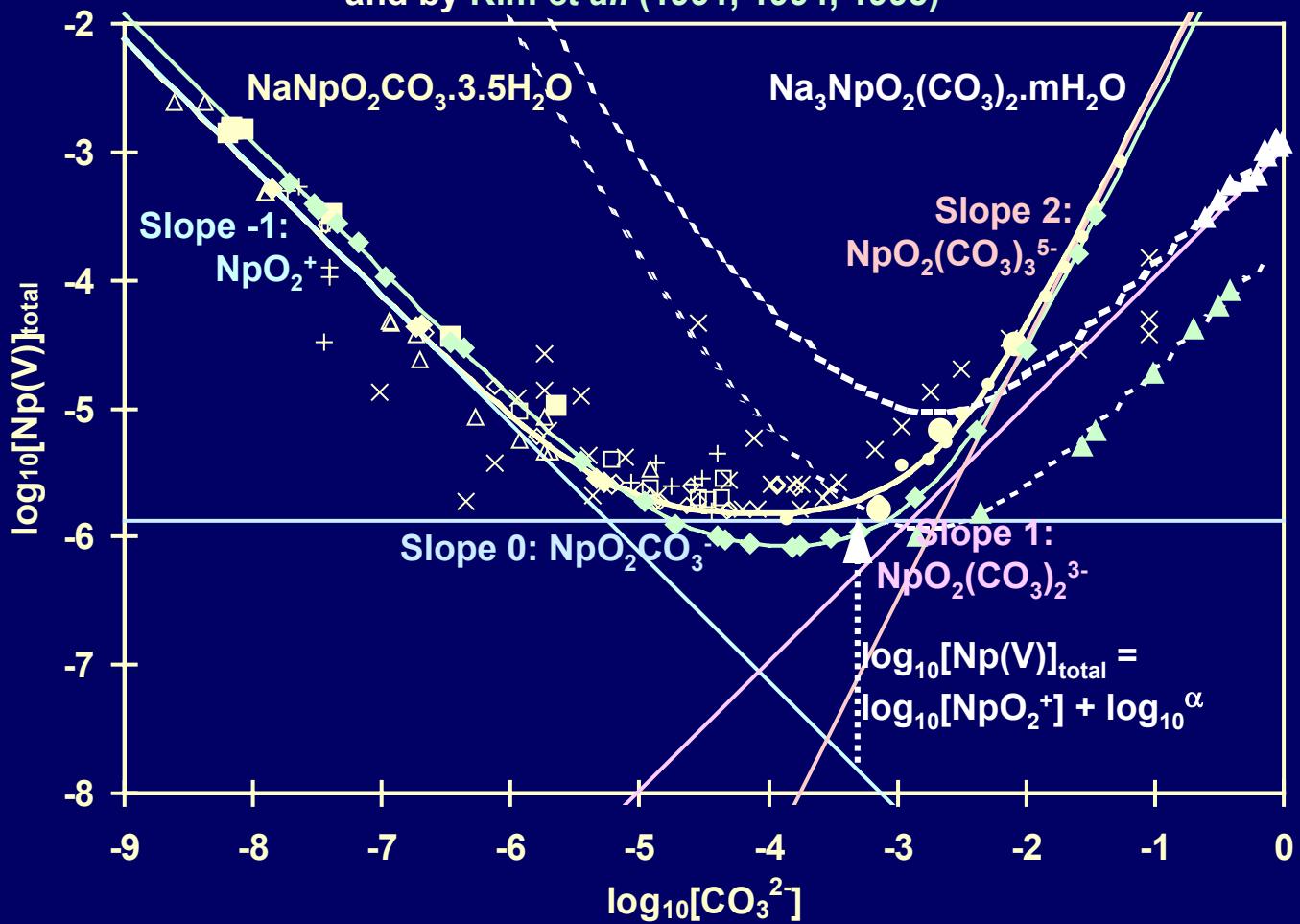
4 - Uranium in natural waters

Oklo and Pyrénées

M.-H.Fauré, C.Beaucaire

Np(V) Solubility in 3M Na^+ aqueous solutions

measured by Simakin (1977), Vitorge et al. (1984, 1985, 1986, 1991, 1998)
 and by Kim et al. (1991, 1994, 1995)



Wait for equilibrium achievement:

Reach equilibrium from both sides, several times,

Characterise solid phase (X-ray diffraction) when equilibrium is obtained.

Control aqueous speciation (including activity coefficients, junction potential)

Mass action law is valid for this ideal system (Slope -1 for NpO_2^+):

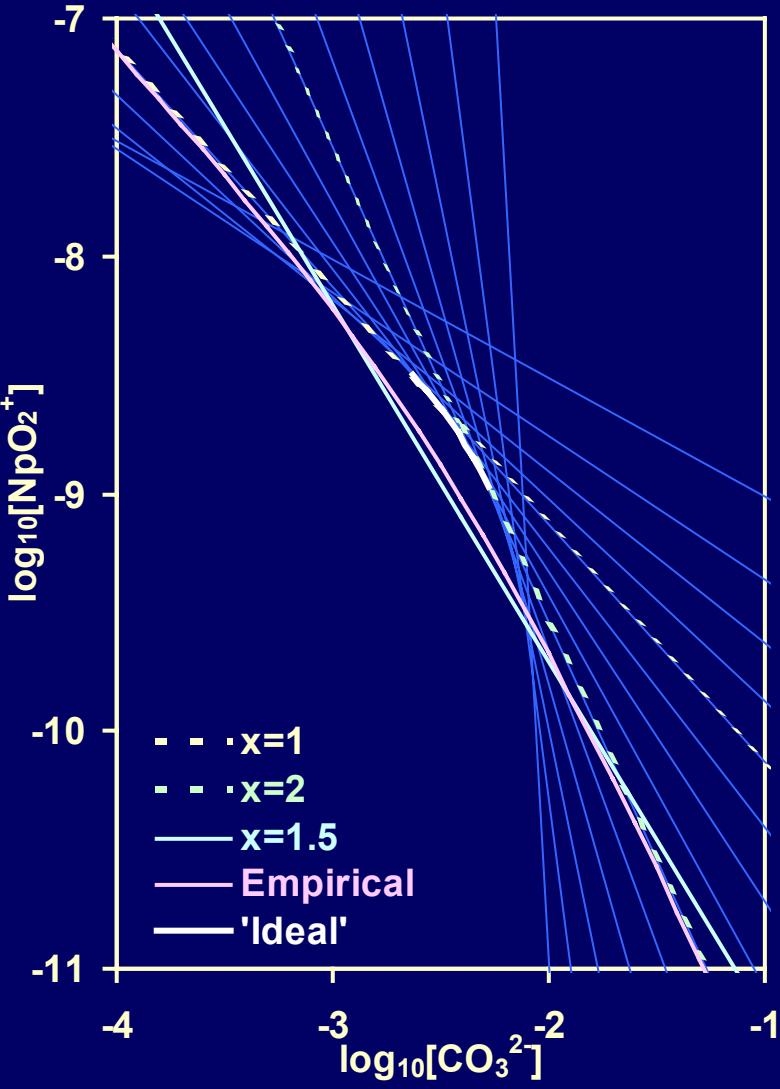
in solid (constant activity), and in solution (constant activity coefficient)

Slow transformation (for $\log_{10}[\text{CO}_3^{2-}] = -2.4$ at equilibrium):



Further slow transformations in both compounds

$\text{Na}_{(2-y)}(\text{NpO}_2)_y\text{CO}_3$ Solid Solution?



$$K_{s1} = [\text{Na}^+] [\text{NpO}_2^+] [\text{CO}_3^{2-}]$$

$$K_{s2} = [\text{Na}^+]^3 [\text{NpO}_2^+] [\text{CO}_3^{2-}]^2$$

$$K_{s1.5} = [\text{Na}^+]^2 [\text{NpO}_2^+] [\text{CO}_3^{2-}]^{1.5}$$

$$v K_{s1} = [\text{Na}^+] [\text{NpO}_2^+] [\text{CO}_3^{2-}]$$

$$(1-v) K_{s2} = [\text{Na}^+]^3 [\text{NpO}_2^+] [\text{CO}_3^{2-}]^2$$

$$\frac{1}{v} = 1 + [\text{Na}^+]^2 [\text{CO}_3^{2-}] \frac{K_{s1}}{K_{s2}}$$

$$K_y = \frac{\chi_{\text{Na}}^{2-y} \chi_{\text{NpO}_2}^y \chi_{\text{CO}_3}}{[\text{Na}^+]^{2-y} [\text{NpO}_2^+]^y [\text{CO}_3^{2-}]}$$

$$K_y = K_1^{2-y} K_2^{y-1} \text{ (see Michard 1989)}$$

$$D = \frac{\chi_{\text{Na}} [\text{Na}^+]}{\chi_{\text{NpO}_2} [\text{NpO}_2^+]} = \frac{K_2}{K_1}$$

$$\chi_{\text{Na}} = (2-y) \chi_{\text{CO}_3}$$

$$\chi_{\text{NpO}_2} = y \chi_{\text{CO}_3}$$

$$\chi_{\text{CO}_3} = \frac{1}{3}$$

$$K_1 = \frac{1}{9 K_{s1}}$$

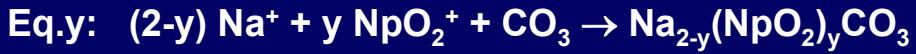
$$K_2 = \frac{0.1443}{\sqrt{K_{s2}}}$$

$$\left(\frac{\partial [\text{NpO}_2^+]}{\partial x} \right)_{[\text{Na}^+], [\text{CO}_3^{2-}]} = 0, \quad \text{where } x = \frac{1}{y}$$

$$\left(\frac{\partial \ln[\text{NpO}_2^+]}{\partial \ln[\text{CO}_3^{2-}]} \right)_{[\text{Na}^+]} = -x$$

Hypothesis: $\mu_{\bar{X}} = \mu_X^\circ + RT \ln \chi_x$ for $X = \text{Na}, \text{NpO}_2$ and CO_3

Thermodynamics of coprecipitation for $\text{Na}_{2-y}(\text{NpO}_2)_y\text{CO}_3$



$\text{Eq.y} = u \text{ Eq.y}_1 + (1-u) \text{ Eq.y}_2,$

$$\text{Eq.D} = t (\text{Eq.y}_1 - \text{Eq.y}_2), \quad u = t (y_1 - y_2), \quad t = 1 / (y_1 - y_2)$$



Hypothesis: $\mu_{\bar{X}} = \mu_X^\circ + RT \ln \chi_X$, for $X = \text{Na}, \text{NpO}_2$ and CO_3 ,

$$\delta_X = \mu_{\bar{X}} - \mu_X, \quad \chi_{\text{Na}} = (2-y) \chi_{\text{CO}_3}, \quad \chi_{\text{NpO}_2} = y \chi_{\text{CO}_3}, \quad \chi_{\text{CO}_3} = 1/3$$

Mass action law for stoichiometric compounds (fixed y_i)

$$0 = d\Delta_r G = \sum (\mu_i d\eta_i) = (\sum \mu_i v_i) d\xi, \quad 0 = \Delta_r G_{K_i}^\circ + RT \ln K_i$$

$$\Delta_r G_{K_i}^\circ = (2 - y_i) \delta_{\text{Na}}^\circ + y_i \delta_{\text{NpO}_2}^\circ + \delta_{\text{CO}_3}^\circ = -RT \ln K_i$$

$$K_i = K_{y_i} = (2y_i - 1)^{2y_i-1} y_i^{y_i} \chi_{\text{CO}_3}^3 K_{si}^{-y_i}, \quad K_{si} = [\text{Na}^+]^{\frac{2}{y_i}-1} [\text{NpO}_2^+] [\text{CO}_3^{2-}]^{\frac{1}{y_i}}$$

Mass action law for solid solution

$$0 = d\Delta_r G = (\sum \mu_i v_i) d\xi + \left(\sum \mu_i \frac{dv_i}{dy} \right) dy$$

$$\sum \mu_i v_i = \Delta_r G_{K_y}^\circ + RT \ln K_y = RT \ln (K_y K_1^{-u} K_2^{-1+u})$$

$$\Delta_r G_{K_y}^\circ = (2 - y) \delta_{\text{Na}}^\circ + y \delta_{\text{NpO}_2}^\circ + \delta_{\text{CO}_3}^\circ = -RT \ln (K_1^u K_2^{1-u})$$

$$K_y = \left(\frac{\chi_{\text{Na}}}{[\text{Na}^+]} \right)^{2-y} \left(\frac{\chi_{\text{NpO}_2}}{[\text{NpO}_2^+]} \right)^y \frac{\chi_{\text{CO}_3}}{[\text{CO}_3^{2-}]}$$

$$\sum \mu_i \frac{dv_i}{dy} = (\Delta_r G_D^\circ + RT \ln D) dy = RT \ln (D K_2^t K_1^{-t})$$

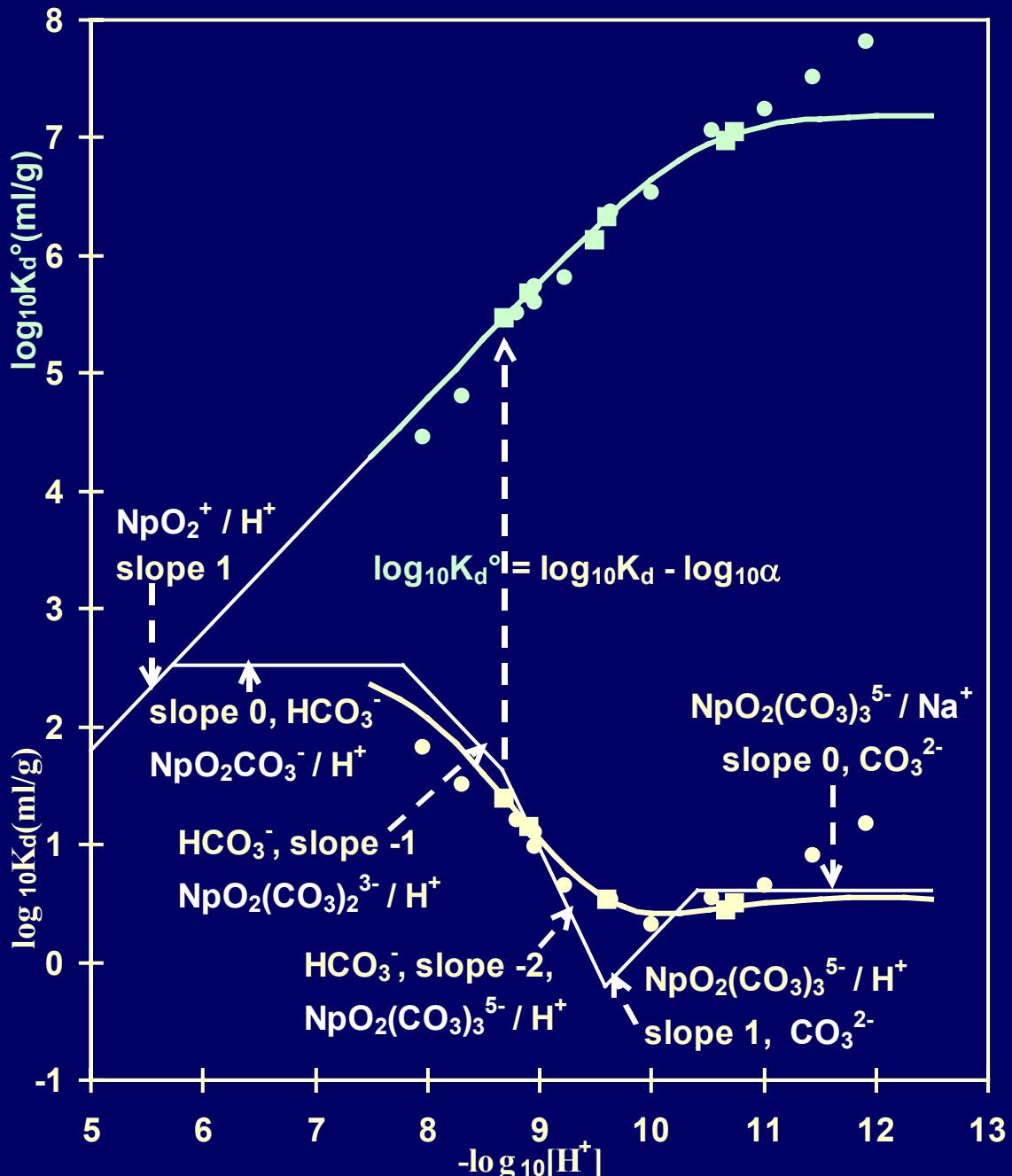
$$\Delta_r G_D^\circ = \delta_{\text{NpO}_2}^\circ - \delta_{\text{Na}}^\circ = t \Delta_r G_{K_1}^\circ - t \Delta_r G_{K_2}^\circ = -t RT \ln (K_1 K_2^{-1})$$

$$D = \frac{[\text{Na}^+] \chi_{\text{NpO}_2}}{[\text{NpO}_2^+] \chi_{\text{Na}}} = \frac{K_1^t}{K_2^t}$$

$$0 = \ln \frac{K_y}{K_1^u K_2^{1-u}} d\xi + \ln \frac{D}{K_1^t K_2^{-t}} dy$$

Np(V) sorption on a clayey sand: $\text{NpO}_2^+/\text{H}^+$ ionic exchange

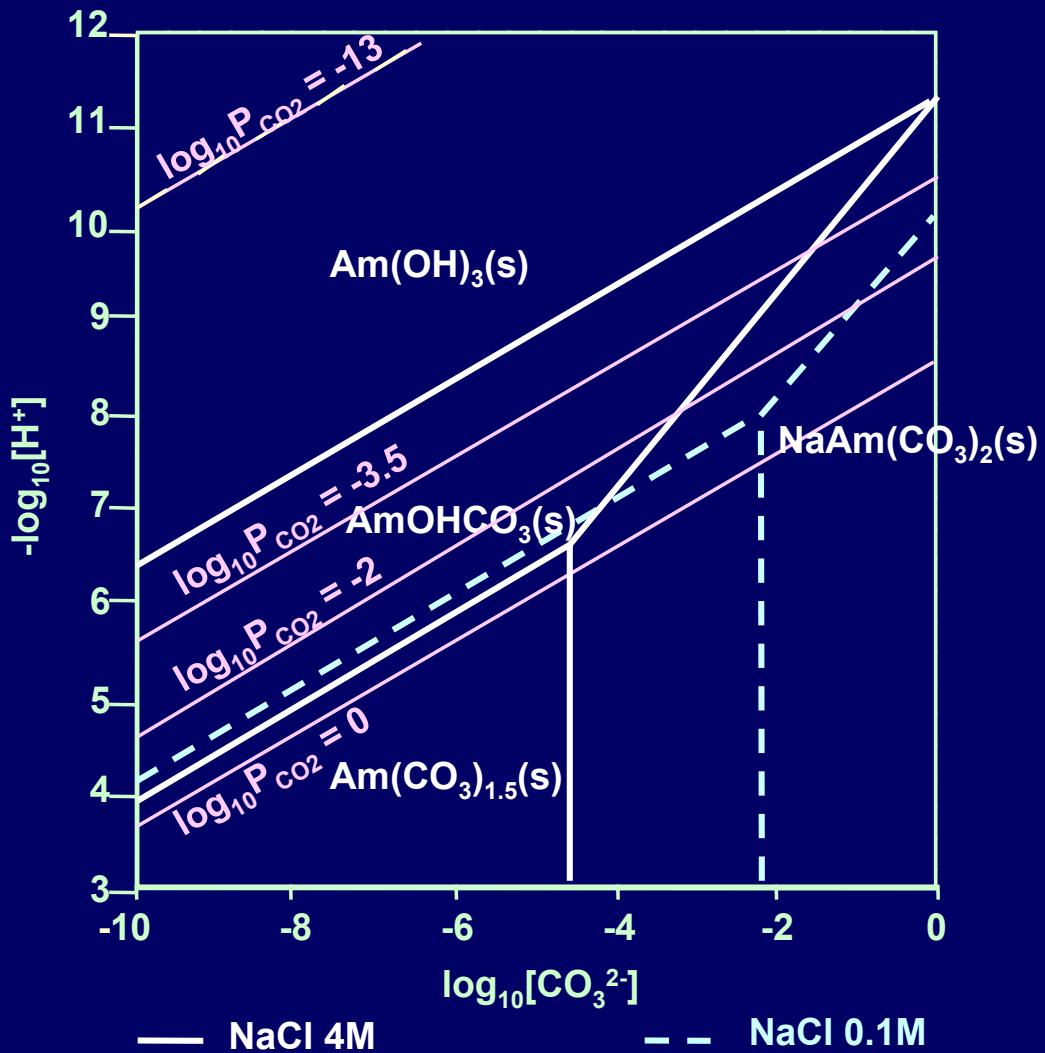
André 1997 (Thesis)



Np(V) is eluted with 1M Na^+ , 0.2M $(\text{HCO}_3^- + \text{CO}_3^{2-})$, ClO_4^- aqueous solutions. Partition coefficient K_d is measured by column experiments, K_d° is NpO_2^+ partition coefficient obtained from K_d and the complexation coefficient α , calculated from complexation constants (known independently).



Vitorge (1992)

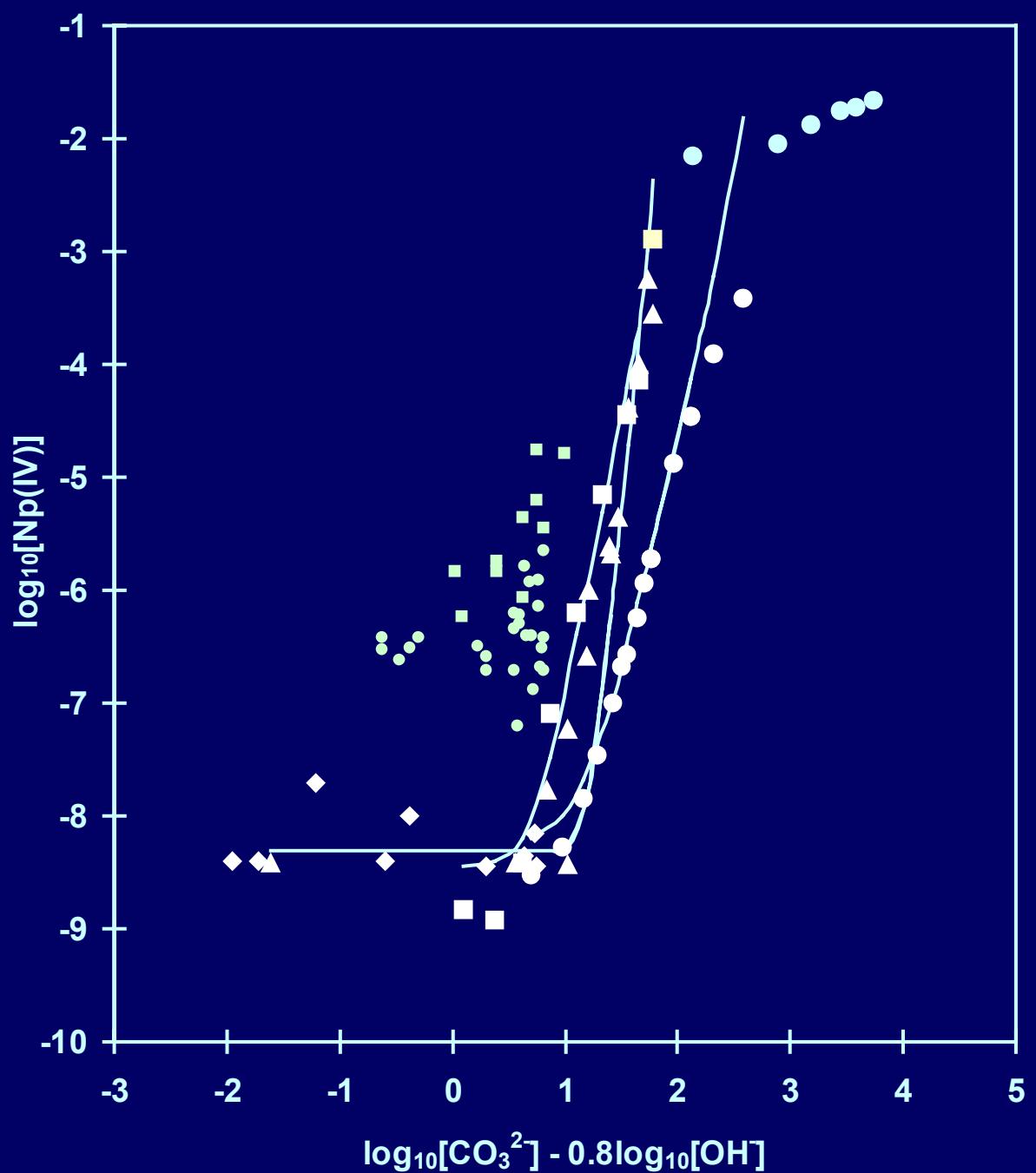


This diagram is from Giffaut *et al.* (1993, 1994), and accepted by TDB (1995)
 Ligand competition in solid phases,
 CO_2 partial pressure (P_{CO_2} , atm) is the key parameter.

Aqueous speciation cannot be deduced from solubility measurements
 equilibrated with air.

Np(IV) solubility in neutral and carbonate aqueous solutions

Measured by

Moskvin (1971), Rai *et al.* (1985, 1999), Prapoto (1989, 1990) and Li *et al.* (1993)

● [71MOS5]

■ [99RAI/HES] KOH

● [99RAI/HES] carbonate

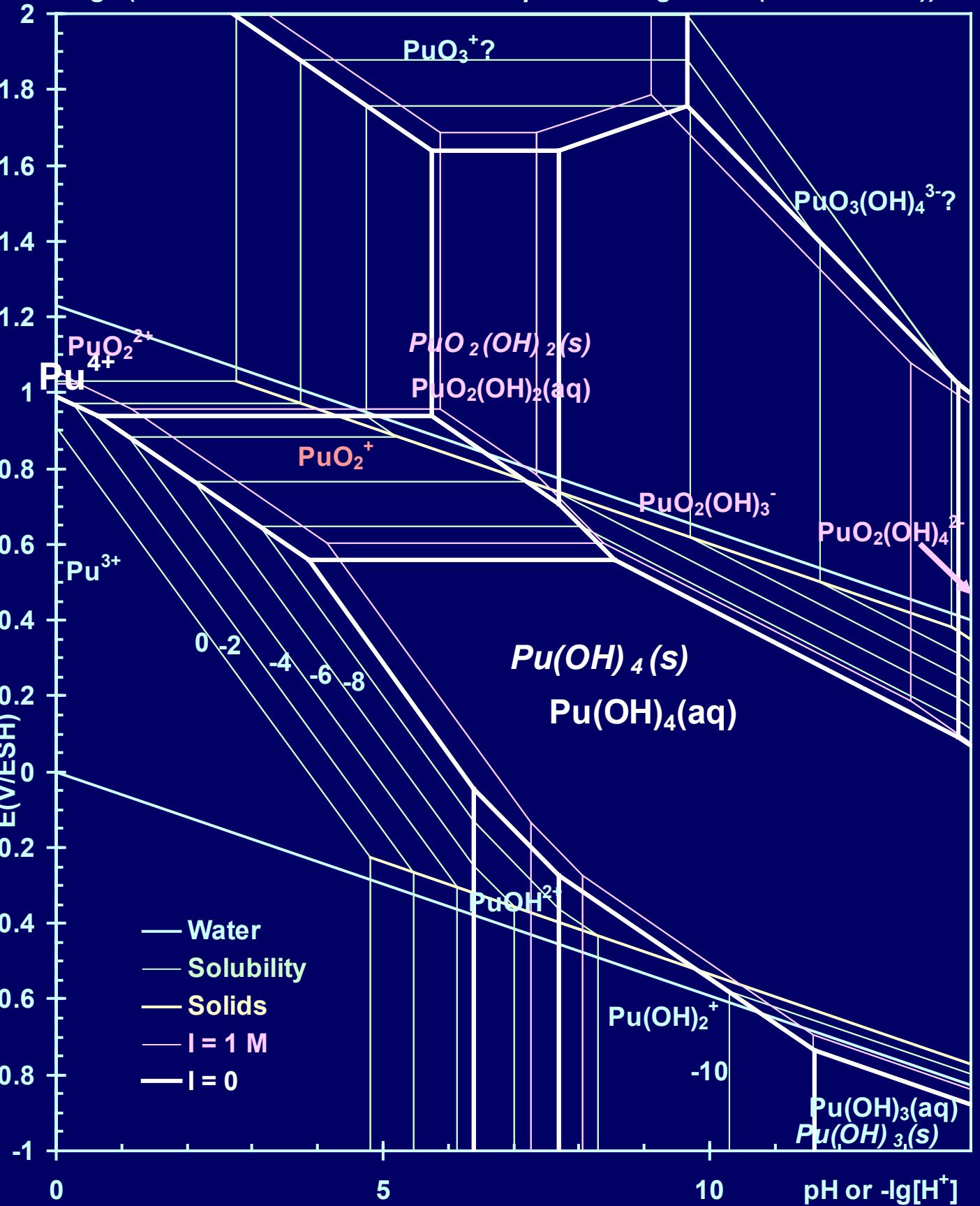
• [90PRA/MOR]

◆ [85RAI/RYA]

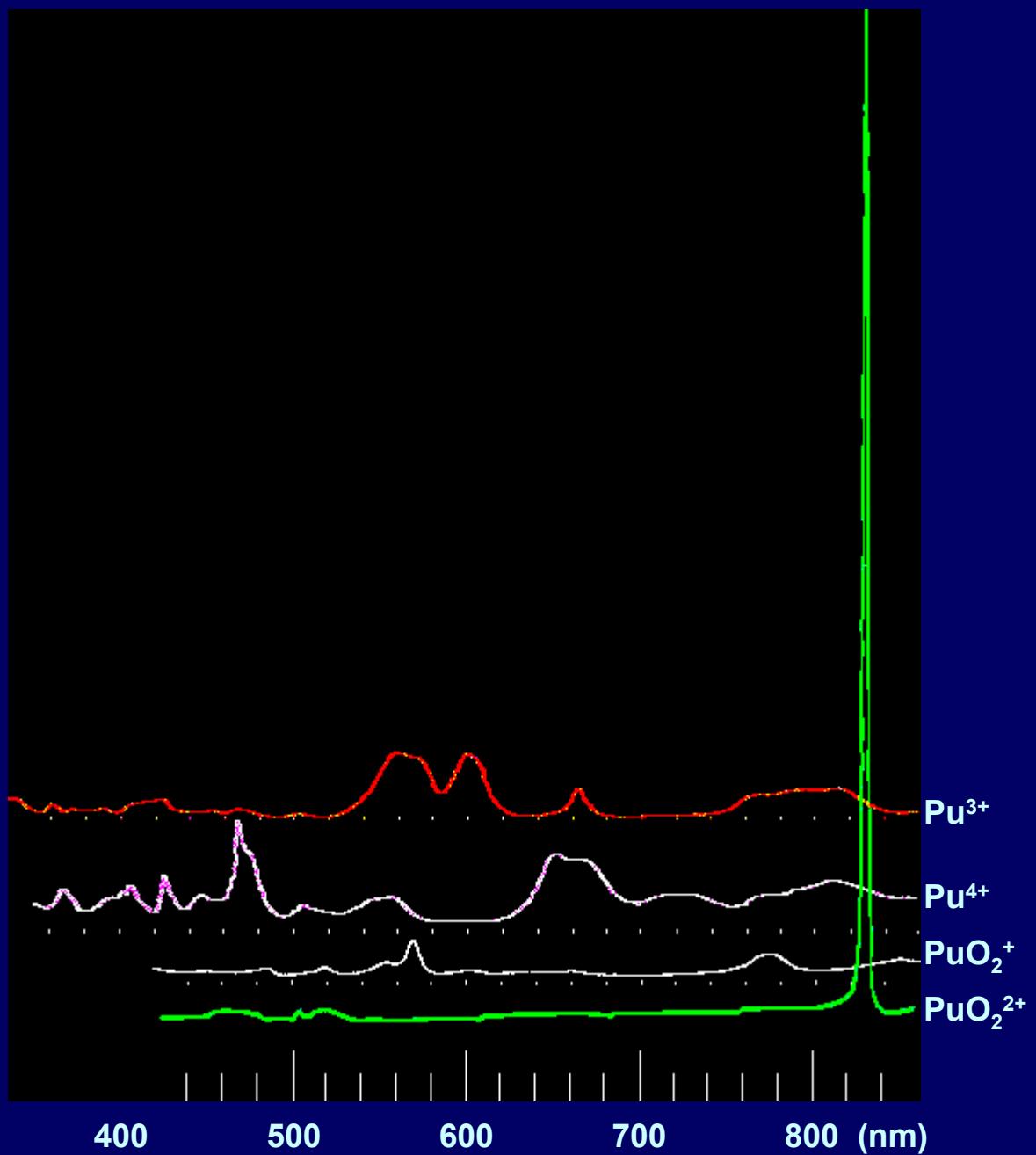
▲ [99RAI/HES] bicarbonate

■ [93LI/KAT]

■ [89MOR/PRA]

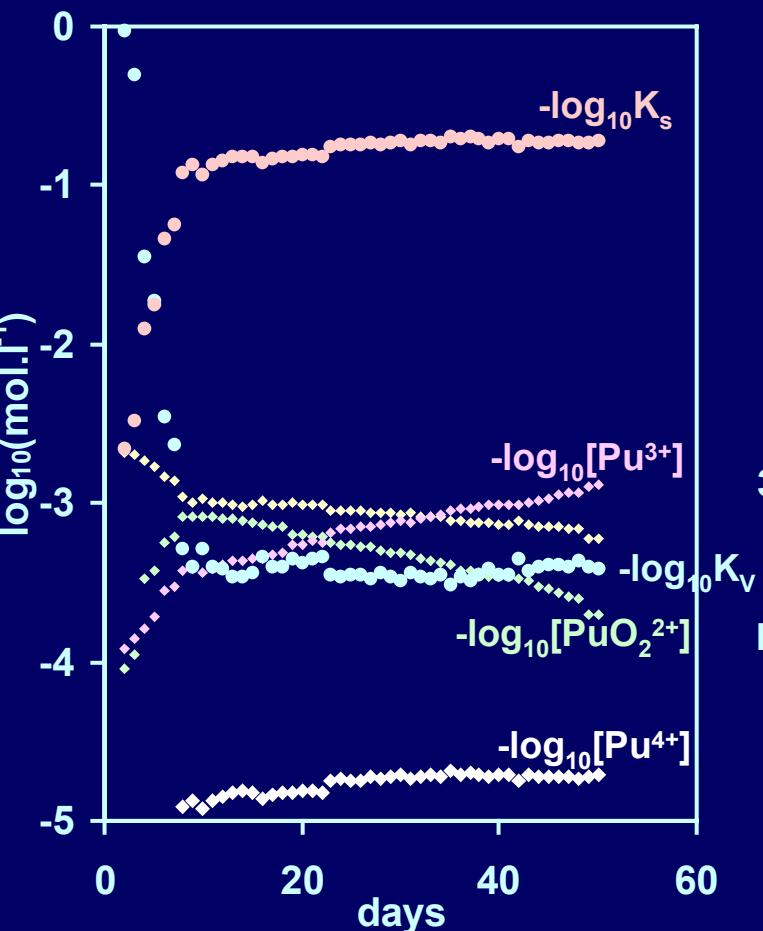
Vitorge (Chimie des actinides *in Techniques de l'ingénieur* (1999 or 2000))

Pu absorption spectra in 1 M HClO_4 aqueous solutions



Pu(IV) solubility in acidic aqueous solutions

Capdevila's thesis (1992), Capdevila et al. (1992, 1995, 1998)



- $-\log_{10}[\text{PuO}_2^{2+}]$
- $-\log_{10}[\text{PuO}_2^+]$
- $-\log_{10}[\text{Pu}^{4+}]$
- $-\log_{10}[\text{Pu}^{3+}]$
- $-\log_{10}K_V$
- $-\log_{10}K_s$



$$K_V = \frac{[\text{PuO}_2^{2+}]^2 [\text{Pu}^{3+}]}{[\text{PuO}_2^+]^3 [\text{H}^+]^4} = 10^{3.44 \pm 0.08}$$

$$E = E_{6/5}^o + 0.05916 \log_{10} \frac{[\text{PuO}_2^{2+}]}{[\text{PuO}_2^+]} = 0.902 \pm 0.009,$$

$$[\text{Pu}^{4+}] = [\text{Pu}^{3+}] 10^{\frac{E - E_{4/3}^o}{0.05916}} = 10^{-4.72 \pm 0.03}$$

$$K_{so} = \frac{[\text{Pu}^{4+}]}{[\text{H}^+]^4} = 10^{-0.72 \pm 0.03}$$

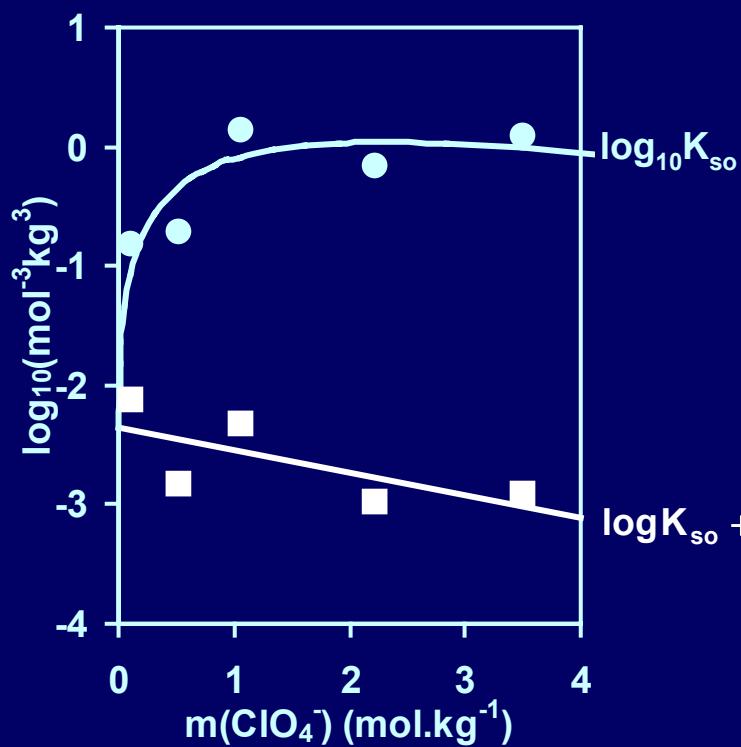


$$\frac{E_{6/5}^o - E_{4/3}^o}{0.05916} - \log_{10} K_s^o = \log_{10} \frac{[\text{PuO}_2^+] [\text{H}^+]^4}{[\text{Pu}^{3+}] [\text{PuO}_2^{2+}]} = 10^{-0.64 \pm 0.03}$$





Capdevila et al. (1998)



$$K_{\text{so}} = \frac{[\text{Pu}^{4+}]}{[\text{H}^+]^4}$$

$$\log K_{\text{so}} + 12 \frac{0.509 \sqrt{I_m}}{1 + \sqrt{I_m}} = \log K_{\text{so}}^\circ - \Delta \varepsilon m_{\text{ClO}_4^-}$$

I_m = ionic strength ($\text{mol} \cdot \text{kg}^{-1}$)

Fitted values:

$$\log K_{\text{so}}^\circ = -2.26 \pm 0.44$$

$$\Delta \varepsilon = 0.27 \pm 0.23$$

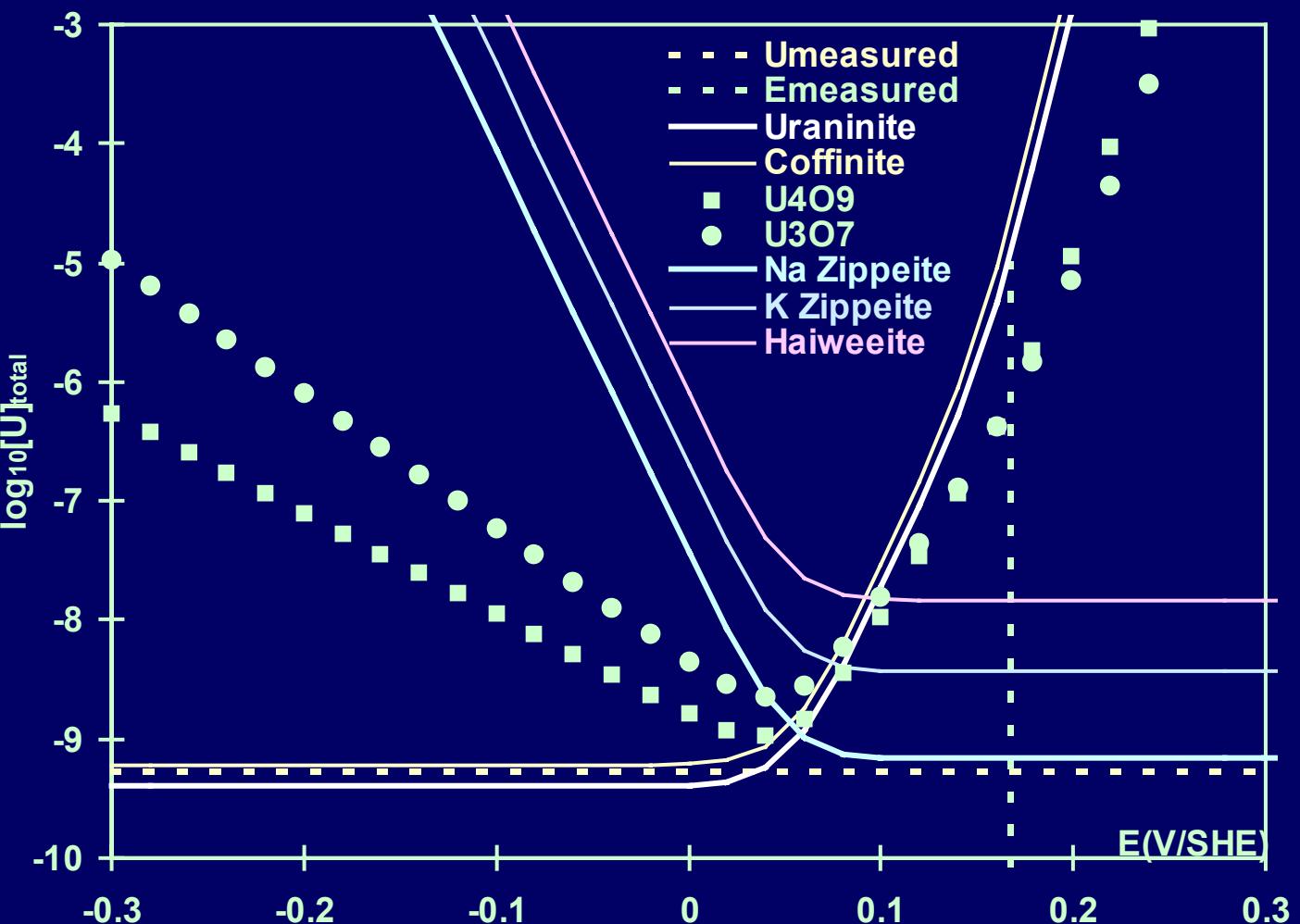
$$\varepsilon(\text{Pu}^{4+}, \text{ClO}_4^-) = 0.89 \pm 0.27$$

$$\text{known value : } 0.82 \pm 0.06$$

Composition of an Oklo natural water Okelobondo (OK195-46)

E	0.167	V/SHE
pH	6.4	
Alkalinity	0.917	mM
U	$5.46 \cdot 10^{-10}$	M
F	0.789	μM
Cl	9.00	μM
S	21.5	μM
P	0.161	μM
Si	0.406	mM
Li	1.45	μM
Na	0.198	mM
K	20	μM
Mg	0.181	mM
Ca	0.125	mM
Ba	0.0874	μM
Fe	0.234	mM
Al	2.68	μM

Uranium solubility in an Oklo natural water (OK195-46)



$\text{UO}_3(\alpha)$ UO_2CO_3 (Rutherfordine)

$\text{UO}_3(\beta)$ $\text{UO}_2\text{CO}_3 \cdot \text{H}_2\text{O}$ (sharpite)

$\text{UO}_3 \cdot 2\text{H}_2\text{O}$

$\text{Ca}(\text{UO}_2)_6\text{O}_4(\text{OH})_6 \cdot 8\text{H}_2\text{O}$ (becquerilite)

$\text{Ca}_3\text{Mg}_3(\text{UO}_2)_2(\text{CO}_3)_6(\text{OH})_4 \cdot 18\text{H}_2\text{O}$ (rabbittite)

$\text{Ca}_3\text{NaUO}_2(\text{CO}_3)_3\text{F}(\text{SO}_4) \cdot 10\text{H}_2\text{O}$ (schroeckingite)

$\text{Na}_4(\text{UO}_2)_6(\text{SO}_4)_2 \cdot 4\text{H}_2\text{O}$ (Na zippeite)

$\text{K}_4(\text{UO}_2)_6(\text{SO}_4)_3(\text{OH})_{10} \cdot 4\text{H}_2\text{O}$ (K zippeite)

$\text{Ca}(\text{UO}_2)_2(\text{Si}_2\text{O}_5)_3 \cdot 5\text{H}_2\text{O}$ (haiweeite)

$\text{Na}_2(\text{UO}_2)_2(\text{Si}_2\text{O}_5)_3 \cdot 4\text{H}_2\text{O}$ (Na-weeksite)

$\text{Ca}(\text{UO}_2)_2(\text{SiO}_3\text{OH})_2$ (uranophane)

U_3O_8

U_3O_7

U_4O_9

$\text{UO}_2(\text{Uraninite})$

$\text{Mg}_2\text{UO}_2(\text{CO}_3)_3 \cdot 18\text{H}_2\text{O}$ (bayleyite)

$\text{CaMgUO}_2(\text{CO}_3)_3 \cdot 12\text{H}_2\text{O}$ (swartzite)

$\text{Ca}_2\text{UO}_2(\text{CO}_3)_3 \cdot 10\text{H}_2\text{O}$ (liebigite)

$\text{CaNa}_2\text{UO}_2(\text{CO}_3)_3 \cdot 6\text{H}_2\text{O}$ (andersonite)

$\text{K}_3\text{NaUO}_2(\text{CO}_3)_3 \cdot \text{H}_2\text{O}$ (grimselite)

$(\text{UO}_2)_3(\text{OH})_2(\text{SO}_4)_2 \cdot 8\text{H}_2\text{O}$

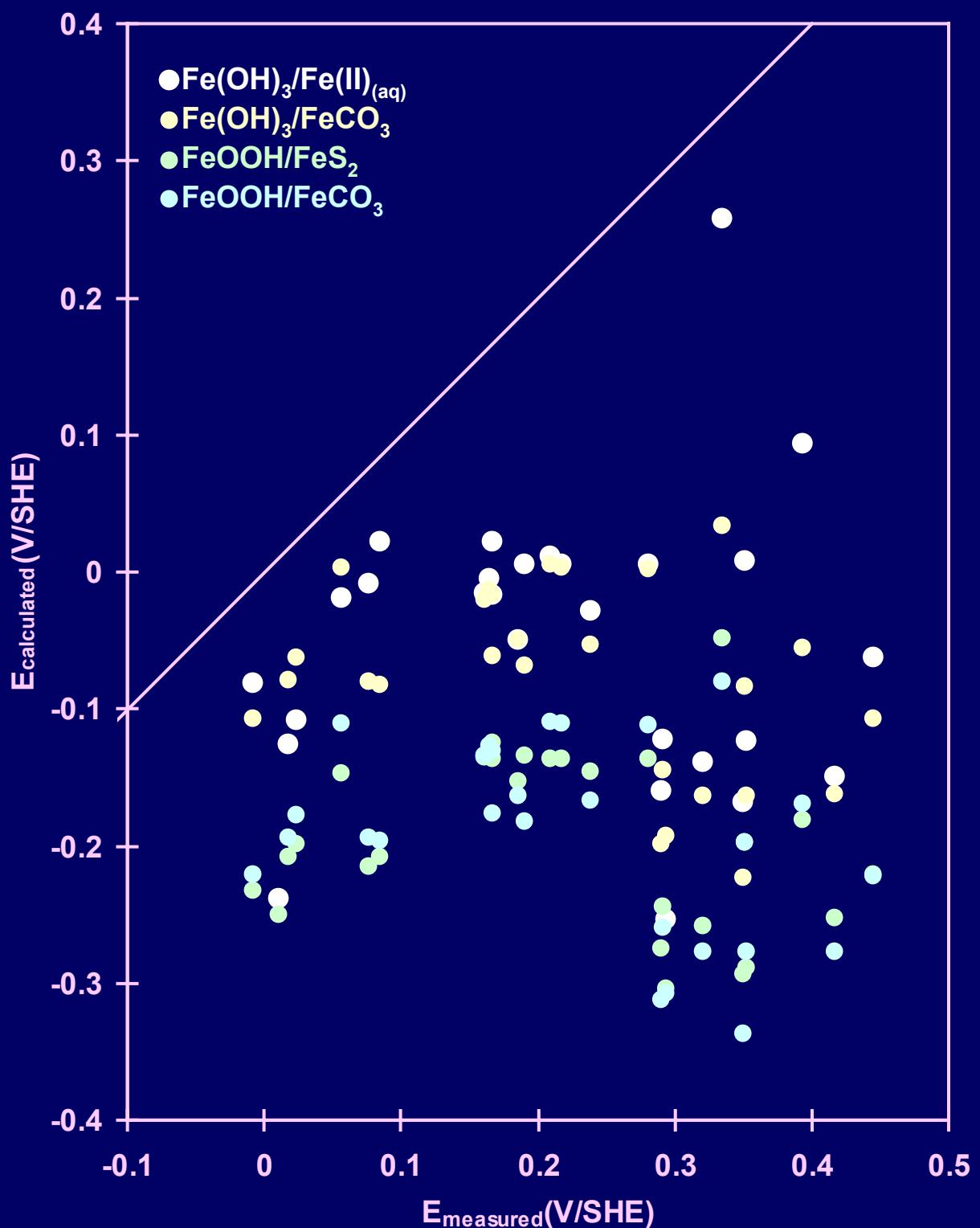
$\text{UO}_2\text{SO}_4 \cdot 3\text{H}_2\text{O}$

$(\text{UO}_2)_2\text{SiO}_4 \cdot 2\text{H}_2\text{O}$ (soddyite)

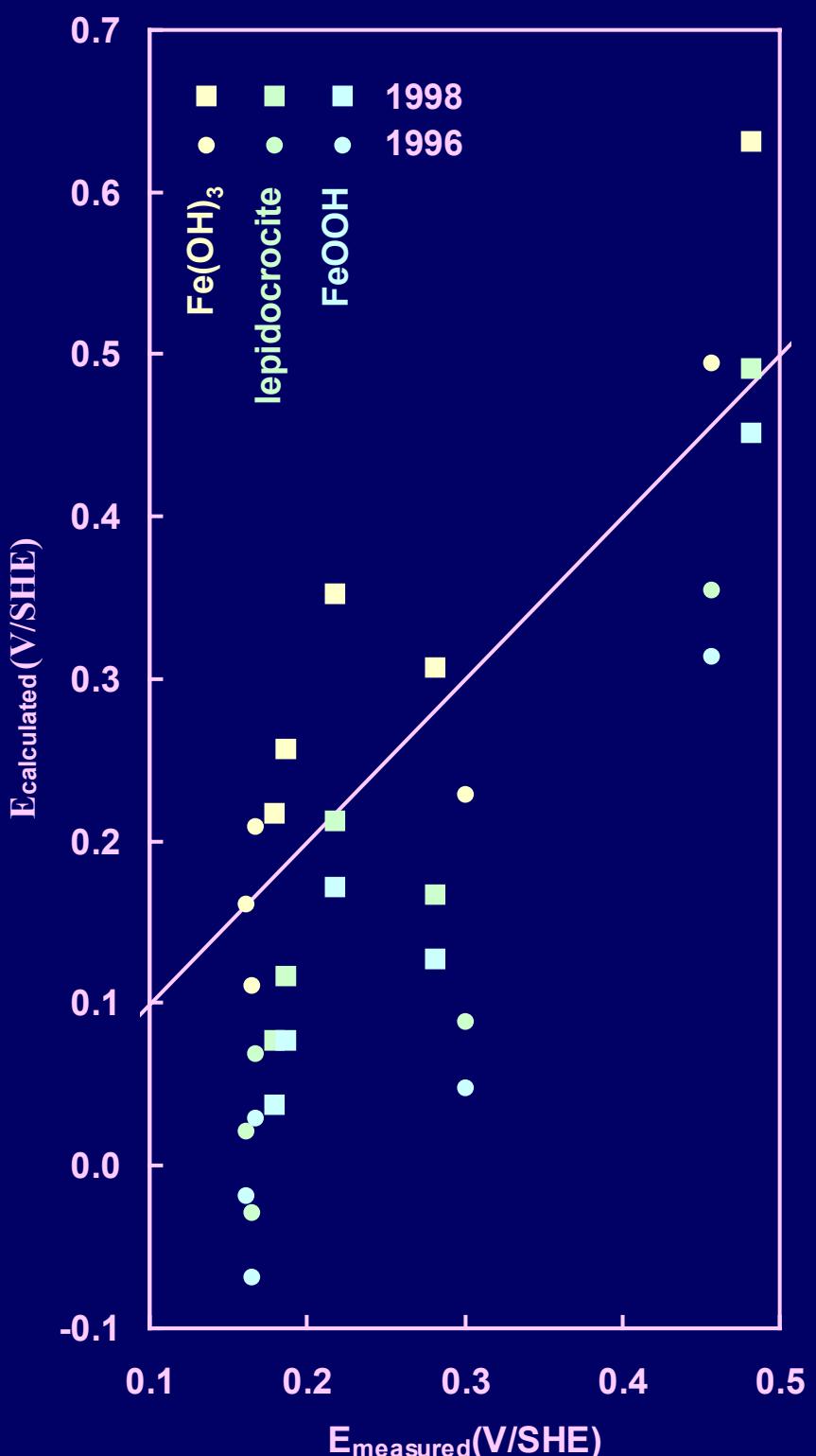
$\text{NaH}_3\text{OUO}_2\text{SiO}_4 \cdot 2\text{H}_2\text{O}$ (naboltwoodite)

USiO_4 (coffinite)

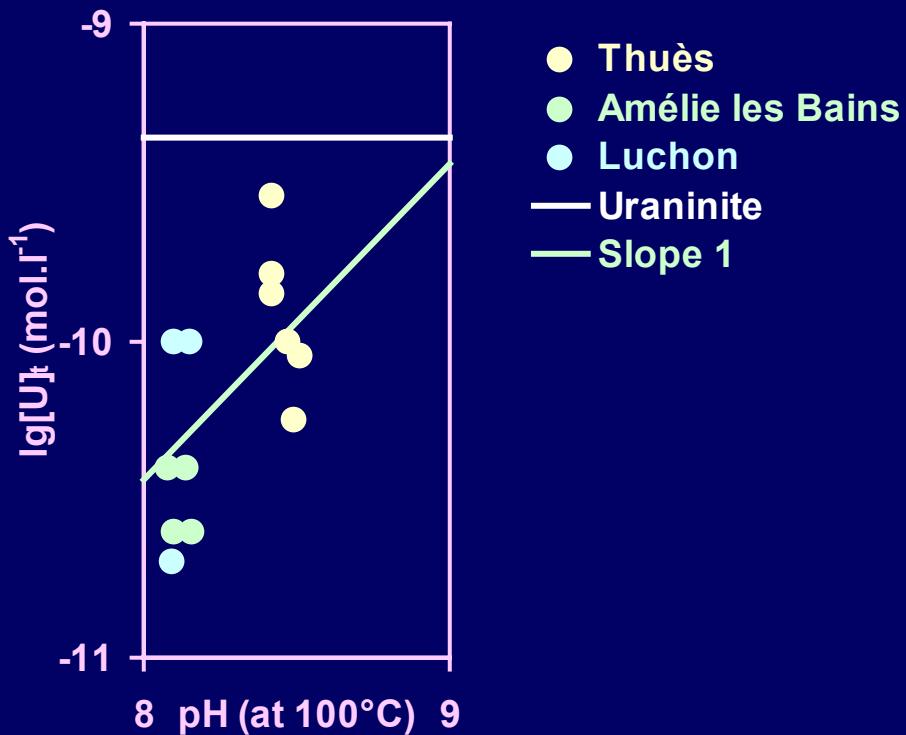
Redox potential in an Oklo natural water (Okelobondo)



Redox potential in an Oklo natural water (Bagombe)



Uranium solubility in Pyrénées waters



Experimental solubility is lower: sorption? New solid phase?

Slope 1?



Typically:

